

After specifying the rule base, the zFLC is ready for execution. During execution, each z-level (i.e., four in our case) is computed in parallel (subject to computational resources) and the output of each individual z-level is recommended to produce the overall result, as explained in Chapter 7. The

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Introduction to Type-2 Fuzzy Logic Control: Theory and Applications, First Edition.

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