

References*

- 12.5.4. Consider the sequence $\alpha = (x_0, x_1, \dots, x_{n-1})$. Let $x_i \equiv x_j \pmod{r}$ if there are two elements in the sequence which are congruent mod r , i.e., $x_i \equiv x_j \pmod{r} \iff x_i - x_j \equiv 0 \pmod{r}$ ($n > m$).
 12.5.5. We have $\alpha \in C$ if and only if $\alpha \in \langle 1 \rangle$. So C is a perfect code. (Since $\alpha \in \langle 1 \rangle$, we must have $A > 1$.) A trivial example for $r = 3$ is the cyclic code $\langle 1, 25 \rangle$. Here we have taken $m = 3^3 - 1$ and $A = 13$.
- The subgroup generated by 3 in \mathbb{F}_3 has index 4 and the coset representatives are $\{1\}$ and $\{2\}$.
- 12.5.6. We have $\alpha \in C$ if and only if $\alpha \in \langle 1 \rangle$. So C is a perfect code. (Since $\alpha \in \langle 1 \rangle$, we must have $A > 1$.) A trivial example for $r = 3$ is the cyclic code $\langle 1, 25 \rangle$. Here we have taken $m = 3^3 - 1$ and $A = 13$.
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12.5.5. In Theorem 12.5.4 it is shown how this situation can arise. Let $f(x) = x^4 + x + 1$ and $g(x)h(x) = x^{12} - 1$. We know that $g(x)$ generates an irreducible polynomial of degree 12 over \mathbb{F}_2 .

12.7.2. In Theorem 12.7.1 it is shown how this situation can arise. Let $f(x) = x^4 + x + 1$ and $g(x)h(x) = x^{12} - 1$. We know that $g(x)$ generates an irreducible polynomial of degree 12 over \mathbb{F}_2 .

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