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The contents of Chapters 14. and 15. refer in part to mathematical knowledge provided in subsequent chapters.