

# APPLIED REGRESSION ANALYSIS & GENERALIZED LINEAR MODELS

3  
EDITION

"The strength of this text is the **unified presentation** of several regression topics that provides the student with a global perspective on regression analysis. The student is well served with this unified approach, as it facilitates deeper research on any one topic with more advanced texts."

—E. C. Hedberg, *Arizona State University*

"This text is a **one-stop shop** for me for my first year stats sequence for students in our program. Those wanting the technical detail will be satisfied; those wanting an **excellent** explanation of these methods using **real-world examples and approachable language** will also be satisfied."

—Corey S. Sparks, *The University of Texas at San Antonio*

"I have **enjoyed** using previous editions of this text and look forward to using this edition. It covers all key topics, and quite a few advanced ones, in one **well-written text**."

—Michael S. Lynch, *University of Georgia*

## PRAISE FOR THE PREVIOUS EDITIONS

"In summary, this is an **excellent** text on regression applications and methods, written with authority, lucidity, and eloquence. The second edition provides substantive and topical updates, and makes the book suitable for courses designed to emphasize both the classical and the modern aspects of regression."

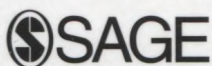
—*Journal of the American Statistical Association*  
(review of the second edition)

"Even though the book is written with social scientists as the target audience, the depth of material and how it is conveyed give it far broader appeal. Indeed, I recommend it as a **useful** learning text and resource for researchers and students in any field that applies regression or linear models (that is, most everyone), including courses for undergraduate statistics majors. The author is to be commended for giving us this book, which I trust will find a wide and enduring readership."

—*Journal of the American Statistical Association*  
(review of the first edition)

"[T]his **wonderfully comprehensive** book focuses on regression analysis and linear models.... We enthusiastically recommend this book—having used it in class, we know that it is thorough and well-liked by students."

—Chance (review of the first edition)



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