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- \* The acquisition of new knowledge only by consideration is characteristic for the mathematics; this makes mathematics to be exact science word for word. Each other science is exact only to the extent, to which it uses just mathematics.

The crucial role in our intention presents Cauchy's functional equation

$$f(x+y) = f(x) + f(y) \quad (0.1)$$