

# Contents

<i>Foreword</i>	page	xiii
<i>Preface</i>	page	xv
<b>Part I Basic Concepts</b>		
<b>1 Introduction</b>	<b>page</b>	<b>1</b>
1.1 Functions	3	
1.2 Functional programming	3	
1.3 Features of Haskell	4	
1.4 Historical background	6	
1.5 A taste of Haskell	8	
1.6 Chapter remarks	9	
1.7 Exercises	13	
<b>2 First steps</b>	<b>page</b>	<b>14</b>
2.1 Glasgow Haskell Compiler	14	
2.2 Installing and starting	14	
2.3 Standard prelude	14	
2.4 Function application	15	
2.5 Haskell scripts	16	
2.6 Chapter remarks	17	
2.7 Exercises	21	
<b>3 Types and classes</b>	<b>page</b>	<b>22</b>
3.1 Basic concepts	22	
3.2 Basic types	23	
3.3 List types	25	
3.4 Tuple types	26	
3.5 Function types	27	
3.6 Curried functions	27	
3.7 Polymorphic types	29	
3.8 Overloaded types	30	
3.9 Basic classes	31	
3.10 Chapter remarks	36	

	3.11 Exercises	36
<b>4</b>	<b>Defining functions</b>	38
4.1	New from old	38
4.2	Conditional expressions	38
4.3	Guarded equations	39
4.4	Pattern matching	40
4.5	Lambda expressions	42
4.6	Operator sections	44
4.7	Chapter remarks	45
4.8	Exercises	45
<b>5</b>	<b>List comprehensions</b>	47
5.1	Basic concepts	47
5.2	Guards	48
5.3	The <code>zip</code> function	50
5.4	String comprehensions	51
5.5	The Caesar cipher	52
5.6	Chapter remarks	56
5.7	Exercises	57
<b>6</b>	<b>Recursive functions</b>	59
6.1	Basic concepts	59
6.2	Recursion on lists	61
6.3	Multiple arguments	63
6.4	Multiple recursion	64
6.5	Mutual recursion	65
6.6	Advice on recursion	66
6.7	Chapter remarks	71
6.8	Exercises	71
<b>7</b>	<b>Higher-order functions</b>	73
7.1	Basic concepts	73
7.2	Processing lists	74
7.3	The <code>foldr</code> function	76
7.4	The <code>foldl</code> function	79
7.5	The composition operator	81
7.6	Binary string transmitter	82
7.7	Voting algorithms	86
7.8	Chapter remarks	89
7.9	Exercises	89
<b>8</b>	<b>Declaring types and classes</b>	92
8.1	Type declarations	92

8.2	Data declarations	8.11	93
8.3	Newtype declarations	8.11	95
8.4	Recursive types	8.11	96
8.5	Class and instance declarations	8.11	99
8.6	Tautology checker	8.11	101
8.7	Abstract machine	8.11	106
8.8	Chapter remarks		108
8.9	Exercises		109

## **9 The countdown problem**

9.1	Introduction	9.81	111
9.2	Arithmetic operators	8.81	111
9.3	Numeric expressions	8.81	112
9.4	Combinatorial functions	8.81	113
9.5	Formalising the problem	8.81	115
9.6	Brute force solution	8.81	115
9.7	Performance testing	8.81	116
9.8	Combining generation and evaluation	8.81	117
9.9	Exploiting algebraic properties	8.81	118
9.10	Chapter remarks	8.81	119
9.11	Exercises	8.81	120

## **Part II Going Further**

### **10 Interactive programming**

10.1	The problem	10.81	123
10.2	The solution	10.81	123
10.3	Basic actions	10.81	124
10.4	Sequencing	10.81	125
10.5	Derived primitives	10.81	126
10.6	Hangman	10.81	127
10.7	Nim	10.81	128
10.8	Life	10.81	129
10.9	Chapter remarks	10.81	133
10.10	Exercises	10.81	137

### **11 Unbeatable tic-tac-toe**

11.1	Introduction	11.81	139
11.2	Basic declarations	11.81	139
11.3	Grid utilities	11.81	140
11.4	Displaying a grid	11.81	141
11.5	Making a move	11.81	142
11.6	Reading a number	11.81	143
11.7	Human vs human	11.81	144

11.8	Game trees	145
11.9	Pruning the tree	147
11.10	Minimax algorithm	148
11.11	Human vs computer	150
11.12	Chapter remarks	151
11.13	Exercises	151
<b>12</b>	<b>Monads and more</b>	
12.1	Functors	153
12.2	Applicatives	157
12.3	Monads	164
12.4	Chapter remarks	174
12.5	Exercises	175
<b>13</b>	<b>Monadic parsing</b>	
13.1	What is a parser?	177
13.2	Parsers as functions	177
13.3	Basic definitions	179
13.4	Sequencing parsers	179
13.5	Making choices	181
13.6	Derived primitives	183
13.7	Handling spacing	186
13.8	Arithmetic expressions	187
13.9	Calculator	191
13.10	Chapter remarks	194
13.11	Exercises	194
<b>14</b>	<b>Foldables and friends</b>	
14.1	Monoids	196
14.2	Foldables	200
14.3	Traversables	206
14.4	Chapter remarks	210
14.5	Exercises	210
<b>15</b>	<b>Lazy evaluation</b>	
15.1	Introduction	212
15.2	Evaluation strategies	213
15.3	Termination	216
15.4	Number of reductions	217
15.5	Infinite structures	219
15.6	Modular programming	220
15.7	Strict application	223
15.8	Chapter remarks	226
15.9	Exercises	226

16

<b>Reasoning about programs</b>	228
16.1 Equational reasoning	228
16.2 Reasoning about Haskell	229
16.3 Simple examples	230
16.4 Induction on numbers	231
16.5 Induction on lists	234
16.6 Making append vanish	238
16.7 Compiler correctness	241
16.8 Chapter remarks	246
16.9 Exercises	246

17

<b>Calculating compilers</b>	249
17.1 Introduction	249
17.2 Syntax and semantics	249
17.3 Adding a stack	250
17.4 Adding a continuation	252
17.5 Defunctionalising	254
17.6 Combining the steps	257
17.7 Chapter remarks	261
17.8 Exercises	261

A

<b>Appendix A Selected solutions</b>	263
A.1 Introduction	263
A.2 First steps	264
A.3 Types and classes	265
A.4 Defining functions	266
A.5 List comprehensions	267
A.6 Recursive functions	267
A.7 Higher-order functions	268
A.8 Declaring types and classes	269
A.9 The countdown problem	270
A.10 Interactive programming	270
A.11 Unbeatable tic-tac-toe	271
A.12 Monads and more	272
A.13 Monadic parsing	273
A.14 Foldables and friends	274
A.15 Lazy evaluation	275
A.16 Reasoning about programs	276
A.17 Calculating compilers	279

B

<b>Appendix B Standard prelude</b>	280
B.1 Basic classes	280
B.2 Booleans	281
B.3 Characters	282

B.4	Strings	Generating sparse bitmaps	283
B.5	Numbers	Drop-in lenses	283
B.6	Tuples	Intersection types	284
B.7	Maybe	Global variables	284
B.8	Lists	Iteration over lists	285
B.9	Functions	Iteration over numbers	285
B.10	Input/output	Iteration over pairs	287
B.11	Functors	Combinator reduction	287
B.12	Applicatives	Combinator evaluation	288
B.13	Monads	Primitives	289
B.14	Alternatives	Cyclically combinable	290
B.15	MonadPlus	Properties	290
B.16	Monoids	Properties	291
B.17	Foldables	Properties	292
B.18	Traversables	Properties	294
	<i>Bibliography</i>	Acknowledgments	297
	<i>Index</i>	Index	300