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This book began as a graduate course that I taught at the University of Colorado in Boulder, for which the prerequisites were undergraduate classical physics and mathematical methods. The primary readership is beginning graduate students, but most of the text ought to be accessible to undergraduates who have had some