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## Web resources

The book's Web site ([www.physics.upenn.edu/biophys/BPse/](http://www.physics.upenn.edu/biophys/BPse/)) contains links to the following resources in the Student section:

- Color figures for those viewing a b/w printout.
- Errata will appear as needed.

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