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Topics in differential equations to a broader mathematical audience, including	
the seminar. The graduation of Ph.D. students has become a rule and	
the seminar are a suitable complement of their study.	
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<i>Jaroslav Milota</i>	
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