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The * in the heading denotes that the section can be skipped on the first reading as it contains background material catered for advanced readers of this book.