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\*Appendix B is online only - please go to [www.wiley.com/go/global/montgomery](http://www.wiley.com/go/global/montgomery) or WileyPlus.