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Bagging

Bootstrap aggregating

BIC

Bayesian information criterion

BFGS

Broyden-Fletcher-Goldfarb-Shanno

BLUE

best linear unbiased estimator

BJ

Box-Jenkins

CMAC

cerebellar model articulation controller

COR-LS

correlation and least squares

DFP

Davidon-Fletcher-Powell

DSFI

discrete square roots filtering in information form

DoE

design of experiments

EA

evolutionary algorithm

ECU

engine control unit

ELS

extended least squares

ES

evolution strategy

FA

fast annealing

FIR

finite impulse response