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17.42 Basic properties of the Mellin transform 17.43 Table of Mellin transforms ansiorms

Bibliographic References Used in Preparation of Text Classified Supplementary References

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