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Brackets

Order

Divide

Multiply

Add

Subtract

$$a^1 = a$$

$$a^2 = a \times a$$

$$a^3 = a \times a \times a$$

$$a^4 = a \times a \times a \times a$$



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